$$f(x,y) = 2x^{3} + 3xy^{2}$$

$$F_{xy} = \int_{0}^{2} f$$

$$\frac{J+}{J} = 6x^2 + 3y^2$$

$$\frac{d^2f}{dx} = 12 \times$$

$$\frac{\int_{3}^{3} f}{\int_{3}^{3} f} = 12$$

6 x y d = 6 y

$$\frac{df}{dx} = 6x + 3y$$

$$6x + 3y = 6y$$

 F_{xy} and F_{yx} don't need to be equal. If there are partial derivatives for every xy then $F_{xy} = F_{yx}$

Laplace

$$U = (x^{2} + y^{2} + z^{2})^{-1} = y^{2} + y^{2} + y^{2} + y^{2} = 0$$

$$\frac{du}{dx} = 2x \cdot \frac{1}{2} (x^{2} + y^{2} + z^{2})^{-2} = -x (x^{2} + y^{2} + z^{2})^{-2} = 0$$

$$\frac{du}{dx} = -1x^{2} + y^{2} + z^{2} + z$$

$$\frac{\partial}{\partial x} = x^{2} \arctan \left(\frac{y}{x}\right) = \frac{\partial^{2}z}{\partial x \partial y} \left(\frac{\partial x}{\partial y}\right) = \frac{\partial y}{\partial x}$$

$$\frac{\partial}{\partial y} = x^{2} \left(\frac{1}{x}\right) = \frac{x^{2}}{x^{2}} = \frac{x^{2}}{x^{2}}$$

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Dx=dx Dy=dy

 $\Delta z = \frac{df}{dx}$ $\Delta x + \frac{df}{dy}$ $\Delta y + \xi_1 \Delta x + \xi_2 \Delta y$ where ξ_1 is partial derivative for Δx and ξ_2 for Δy

 $\Delta z = \frac{\partial f}{\partial x} \partial x + \frac{\partial f}{\partial y} \partial y + \xi_1 \partial_x + \xi_2 \partial_y$

Important Part - Differation of

$$\frac{2}{2} = \frac{1}{2} (x,y) = x^{2}y - 3y = 3 \quad \Delta = \frac{3}{2} \quad d_{2} = \frac{3}{2}$$

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As we seen here when $\Delta \times and \Delta y$ go to O then $\partial \mathcal{L} \subseteq \Delta \mathcal{L}$

du = du dx + du dy ---U= x => du =? dy=(xeyx)dy du=e x/2x+y)dx+exdy Z- (x, y) x-g(r,s) y-h(r,s) of of dx dr ds 2 / X / S $\frac{\partial f}{\partial x} = \frac{\partial f}{\partial x} + \frac{\partial f}{\partial y}$ ds dx ds

$$\frac{dz}{dz} = e^{x} \sin y, \quad x = \ln t, \quad y = t^{2} \quad \frac{dz}{dt} = \frac{1}{1}$$

$$\frac{dz}{dz} = e^{x} \cos y, \quad \frac{dz}{dt} = \frac{1}{1} \frac{dz}{dt} = \frac{1}{1} \frac{dz}{dt}$$

$$\frac{dz}{dt} = \frac{1}{t}$$

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$$e^{x} \left(\frac{\sin y}{t} + \cos y z t \right)$$

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T= x - x 1 + y X=rcosa y=rsina dt dt dt dy dr dT -7 $dT = (3x - 1) \cos \theta + (3y - x) \sin \theta$ $\frac{dT}{dt} = (3x^2 - y) \cdot -rsin \theta + (3y^2 - x) rcos \theta$ 20

$$\frac{dv}{ds} = \frac{1}{\sqrt{1 + 3r^2 + 5}}, \quad y = 4r - 2s^3, \quad z = 2r^2 - 3s^2$$

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$$2 = f(v) \qquad v = xy \qquad \text{Prove that} \qquad x \frac{\partial z}{\partial x} = 2y \frac{\partial z}{\partial y}$$

$$\frac{\partial z}{\partial y} = \frac{\partial z}{\partial y} = \frac{\partial z}{\partial y} = \frac{\partial v}{\partial y}$$

$$\frac{\partial y}{\partial y} = \frac{\partial z}{\partial y} = \frac{\partial v}{\partial y}$$

$$\frac{\partial^{2}}{\partial y} = \frac{1}{24y} \frac{\partial^{2}}{\partial x} - \frac{1}{24y} \frac{\partial^{2}}{\partial x} - \frac{1}{24y} \frac{\partial^{2}}{\partial x} - \frac{1}{24y} \frac{\partial^{2}}{\partial y} -$$

$$x + y = t$$

$$x +$$

$$\frac{dv}{dt} = \frac{1}{x}$$

$$\frac{2(F_{1}G)}{2(v_{1}v_{2})} = |F_{v}| F_{v} | F_{v}$$

$$F(x,y,v,u) = 0 \ (x,y,v,u) = 0$$

$$\frac{\int_{0}^{1} fx \ fu}{\int_{0}^{1} fx \ fu} \ \frac{\int_{0}^{1} fx \ fu}{\int_{0}^{1} fx \ fu}} \ \frac{\int_{0}^{1} fx \ fu}{\int_{0}^{1} fx \$$

$$\frac{\partial^{2} - \partial^{2} - 3x + y}{\partial v - 2v^{2} - x - 2y} = \frac{\partial^{2} v}{\partial x}, \frac{\partial^{2} v}{\partial y}, \frac{\partial^{2} v}{\partial x}, \frac{\partial^{2} v}{\partial y} = \frac{7}{7}$$

$$f(v, v, x, y) = 0 \Rightarrow v^{2} - v - 3x - y = 0$$

$$g(v, v, x, y) = 0 \Rightarrow v - 2v^{2} - x + 2y = 0$$

$$\frac{|F_{x} F_{x} |}{|G_{x} G_{x} |} = \frac{|-3|}{|-1|} - \frac{|2w - 1|}{|-1|} = \frac{|2w - 1|}{|-1|}$$

$$\frac{\partial^{2} v}{\partial x} = -\frac{|F_{y} |F_{y} |}{|G_{y} |G_{x} |} = \frac{|2w - 1|}{|-1|} = \frac{|2w - 1|}{|-1|}$$

$$\frac{dv}{d9} = -\frac{|F_{9}|F_{e}|}{|F_{9}|G_{e}|} = -\frac{|-1|}{|2|G_{e}|} = -\frac{|-1|}{|2|G_{e}|} = -\frac{|-1|}{|2|G_{e}|} = -\frac{|-1|}{|3|G_{e}|} = -\frac{|-1|}{|3|G_{e}$$

$$\frac{\partial o}{\partial x} = -\frac{|f_0|f_x|}{|f_0|f_x|} \frac{|f_0|f_x|}{|f_0|f_x|} \frac{|f_0|f_x|}{$$

$$\frac{du}{dy} = -\frac{|F_0 F_y|}{|G_0 G_y|} = -\frac{|Z_0 - 1|}{|I_0 - 4|} = -\frac{|F_0 F_y|}{|I_0 - 4|} = -\frac{|I_0 - 1|}{|I_0 - 4|}$$

$$\frac{\partial^{2} - x^{2} - y = 0}{\partial x dy} = \frac{\partial^{2} t}{\partial x dy} = \frac{1}{1}$$

$$\frac{\partial t}{\partial x dy} = \frac{\partial}{\partial x} \left(\frac{\partial t}{\partial y} \right)$$

$$\frac{\partial t}{\partial x} = \frac{\partial}{\partial x} \left(\frac{\partial t}{\partial y} \right)$$

$$\frac{\partial t}{\partial y} = \frac{\partial^{2} t}{\partial y} = \frac{\partial^{2} t}{\partial y} = \frac{1}{1} = 0$$

$$\frac{\partial t}{\partial y} = \frac{\partial^{2} t}{\partial y} = \frac{\partial^{2} t}{\partial y} = \frac{\partial^{2} t}{\partial x} = \frac{\partial^{2}$$

-(}F_-X)

is there a connection U=JXy between then? If it's then how? OZ exy +xy Ux Uy | - | 2√xy | 2√xy | 20 | Ux Uy | - - x = +x | -x = +x | So there is a functional connection between u and U てこ メグ 0=exy+xy > 0-e +0=0

X-1050 02/050 0-30 yada ---() \sim \sim \sim \sim 0-0940

2--1

$$(-2; -3+3k) \cdot (\frac{-i+2j+k}{\sqrt{6}})$$

$$T_0 = -2; +2$$

$$=(2-2+3)\frac{1}{56}=\frac{3}{56}=\frac{56}{2}$$

$$T = \frac{1}{2}i + (2si + 1)j + (1 - cos)k$$

$$\frac{dr}{dr} = -\frac{1}{2}i + 2cos + 2i + (1 + si + 1)k$$

$$T_{0} = -\frac{1}{2}i + 2j + k$$

$$T = -\frac{1}{2}i + 2j + k$$

$$T = -\frac{1}{2}i + 2j + k$$

Double |
$$x+y-a|$$
 $y=2x^2$
 $x=1$
 $x=1$

$$y \le 2x, x - y \le 0 \qquad f(x, y) = x^{2} + y$$

$$y = 2x, x - y \le 0$$

$$x = y$$

$$x = y$$

$$x = y$$

$$x = y$$

$$x + y = y$$

$$x = x$$

$$x = y$$

$$x + y = y$$

$$y = \sqrt{3}x$$

$$y =$$

x +y <4x ore or of this? 大十了一4%二〇 2 + 7 - 4 + 4 - 1 X-4X+4+7-4 (+-2) + (-2) = (+-2) + (-2) = y= 14-4 choose y= 4-(x-2) this for ecsi, or 2 L x 2 2 V 9 = (x-2) 454-27 - \[\begin{align*} & \frac{1}{\sum_{2} - \sum_{2}} & \frac{1} $\frac{A}{2}$ レス・ナマ x = asint

$$\frac{1}{\sqrt{4-(2s)^{2}}} = \frac{1}{\sqrt{4-(2s)^{2}}} = \frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}}$$